

Elastic Collisions

Conservation of Momentum

Objective:

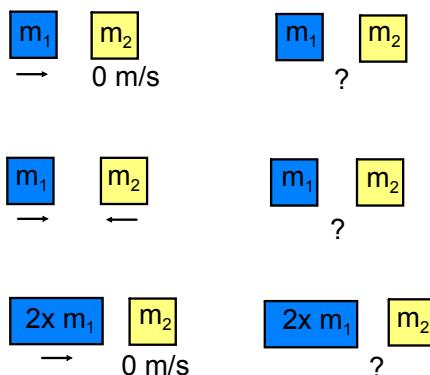
Apply conservation of momentum to elastic collisions.

Identify characteristics of **elastic collisions**.

Calculate final momentum or velocity of objects in an elastic collision.



Before After



Conservation of Momentum

- total momentum is constant in a system
- applies to elastic & inelastic

$$\sum P_b = P_a$$



Elastic Collisions - bounce

- objects follow separate paths
- momentum is transferred between objects

$$\cancel{\sum p_b = p_a}$$

total p before = total p after

$$p_1 + p_2 = p_1' + p_2'$$

$$m_1 \cdot v_1 + m_2 \cdot v_2 = m_1 \cdot v_1' + m_2 \cdot v_2'$$

Elastic Collision Problem

$$m_1 = .4 \text{ kg}$$



$$v_1 = 6 \text{ m/s}$$

$$v_1' = 2 \text{ m/s}$$

$$m_2 = .2 \text{ kg}$$



$$v_2 = 0 \text{ m/s}$$

$$v_2' = ?$$

$$m_1 \cdot v_1 + m_2 \cdot v_2 = m_1 \cdot v_1' + m_2 \cdot v_2'$$

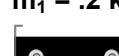
$$(4 \cdot 6) + (.2 \cdot 0) = (.4 \cdot 2) + (.2) v_2'$$

$$2.4 + 0 = .8 + .2 v_2'$$

$$1.6 = .2 v_2'$$

$$(P_f = V_2)$$

$$m_1 = .2 \text{ kg}$$



$$v_1 = 6 \text{ m/s}$$

$$v_1' = -2 \text{ m/s}$$

$$m_2 = .4 \text{ kg}$$



$$v_2 = 0 \text{ m/s}$$

$$v_2' = ?$$

$$m_1 \cdot v_1 + m_2 \cdot v_2 = m_1 \cdot v_1' + m_2 \cdot v_2'$$

$$(.2 \cdot 6) + (.4 \cdot 0) = (.2) (-2) + (.4) v_2'$$

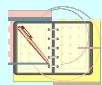
$$1.2 + 0 = -.4 + .4 v_2'$$

$$1.6 = .4 v_2'$$

$$(V_2' = 4 \frac{m}{s})$$

Elastic Collisions

Assignments . . .



- Ch 6 Homework # 11 - 14



Homework Question # 11

$$\begin{array}{c} m_1 \\ \cdot 165 \text{ kg} \\ \xrightarrow{\hspace{1cm}} \\ v_1 = 3.2 \frac{m}{s} \\ v_1' = 0 \end{array}$$

$$\begin{array}{c} m_2 \\ \cdot 165 \text{ kg} \\ v_2 = 0 \\ v_2' = ? \end{array}$$

$$\begin{aligned} m_1 v_1 + m_2 v_2 &= m_1 v_1' + m_2 v_2' \\ (.165)(3.2) + 0 &= 0 + (.165)v_2' \\ .528 &= .165 v_2' \\ v_2' &= 3.2 \frac{m}{s} \end{aligned}$$

Homework Question # 12

$$\begin{array}{c} m_1 \\ 300 \text{ kg} \\ \xrightarrow{\hspace{1cm}} \\ v_1 = 10 \frac{m}{s} \\ v_1' = 4.12 \frac{m}{s} \end{array}$$

$$\begin{array}{c} m_2 \\ 125 \text{ kg} \\ v_2 = 0 \\ v_2' = ? \end{array}$$

a) $p = m_1 v_1$

b) $p = m_1 v_1'$

c)

$$\begin{aligned} m_1 v_1 + m_2 v_2 &= m_1 v_1' + m_2 v_2' \\ 300 \text{ kg} \cdot \frac{m}{s} + 0 &= 1236 \text{ kg} \cdot \frac{m}{s} + 1236 \text{ kg} \cdot \frac{m}{s} \\ &\quad \swarrow \quad \searrow \\ &= 1236 v_2' \end{aligned}$$